

Script Python

Thursday 18 October 2018

22:56

```
from numpy import *  $\rightarrow$  numpy library  
from pylab import *  $\rightarrow$  matplotlib library
```

comment
#I define the parameters

```
Np=300 #Number of grid points  
L=20 #length of the discretized domain  $\rightarrow$  expressed in nm  
W=10 #width of the potential well  $\rightarrow$  in nm  
hbar=1.05459e-34 #J/s  
q=1.60219e-19 #C  
m0=9.1095e-31 #Kg
```

```
#I create the grid  
x=linspace(0,L,Np) # in nanometers
```

nonzero (x > 10)

*you get the indexes of
x > 10*

```
#I create the potential U(x) for the well  
ind=nonzero(abs(x-L*0.5)>W*0.5);  
U=zeros(Np);  $\rightarrow$  absolute value  
U[ind]=10 #The height of the barrier is 10 eV
```

*creates a vector with
Np and equal to 0*

```
# Uncomment these three lines to plot the potential and exit  
plot(x,U,'o-')  
#show()  $\rightarrow$   
#exit(0);
```

```
#I create the hopping parameter  $-\hbar^2/(2m_0 a^2)$   
a=x[1]-x[0]  
t=-hbar**2/(2*m0*(a*1e-9)**2)/q #eV
```

H =

```
#I create the diagonal, updiagonal and lowdiagonal vectors  
diago=(U-2*t)*(ones(Np));  $\rightarrow$  creates a vector of "1", long Np  
lowdiag=t*ones(Np-1);  
updiag=t*ones(Np-1);
```

```
#I create the Hamiltonian  
H=diag(diago)+diag(lowdiag,-1)+diag(updiag,1)  
H=array(H)  
#H=mat(H)
```

*Np x Np matrix, zero everywhere
except in the lowdiag = lowdiag
vector*

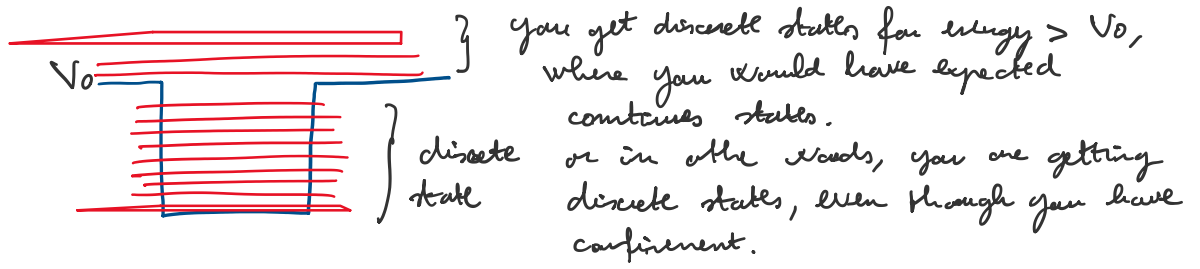
Updiag

*Np x Np matrix
zero everywhere
except in the diag*

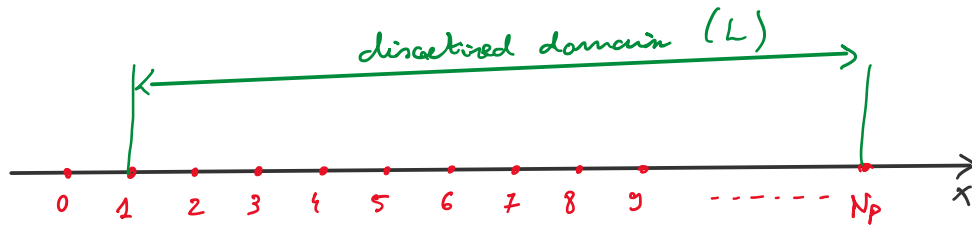
```
[E,V]=eig(H)  $\rightarrow$  computes the eigenvalues  
and the  
print (hbar*q/(m0*W*1e9)**2/2) min(E)
```

eigenvalues

If you run the simulation you get something like this:



What is going on?



for a point $1 < \bar{i} < N_p$
 the Schrodinger equation (discretised)

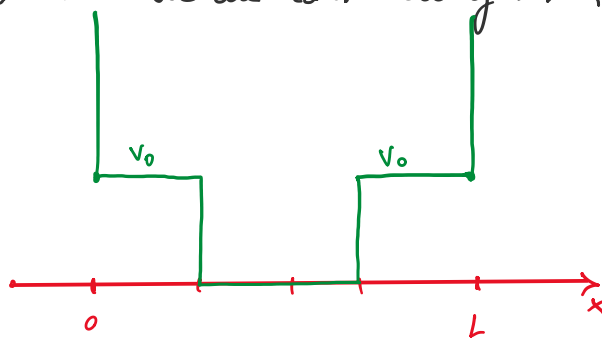
$$t\psi_{i-1} + (U - 2t)\psi_i + t\psi_{i+1} = E\psi_i$$

If $\bar{i} = 1$: $(U - 2t)\psi_i + t\psi_{i+1} = E\psi_i$
 or in other words $\psi_0 = 0$

And in the same way $\psi_{N_p+1} = 0$

$U_0 \rightarrow +\infty$ \wedge $U_{N_p+1} \rightarrow +\infty$, i.e., hard wall assumption

The real potential we are considering is the following:

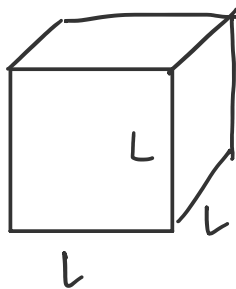


Homework: Compute the eigenvalues and eigenvectors of a harmonic potential and compare results with analytical solution. What is the difference (if any)?

USEFULL RULE

Wednesday, 24 October 2018 15:19

$$I = \sum_{\mathbf{k}} f(\mathbf{k})$$



$$k_x = \frac{2\pi i}{L} \Delta k$$

$$\sum_{\mathbf{k}} f(\mathbf{k}) = \frac{L^3}{(2\pi)^3} \sum_{\mathbf{k}} f(\mathbf{k}) \underbrace{\frac{(2\pi)^3}{L^3}}_{(\Delta k)^3} = \frac{L^3}{(2\pi)^3} \sum_{\mathbf{k}} f(\mathbf{k}) (\Delta k)^3 \quad \Delta k \rightarrow 0$$

$$\Delta k \rightarrow 0 \Rightarrow$$

$$\sum_{\mathbf{k}} f(\mathbf{k}) \rightarrow \frac{L^3}{(2\pi)^3} \int_{\mathbf{k}} f(\mathbf{k}) d^3 k$$

$$d = 1, 2, 3$$

$$\sum_{\mathbf{k}} f(\mathbf{k}) = \textcircled{2} \frac{L^d}{(2\pi)^d} \int_{\mathbf{k}} f(\mathbf{k}) (d k)^d$$

degeneracy of the spin